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Flow structure of subcooled boiling flow in an internally heated annulus

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Abstract

Local measurements of flow parameters were performed for vertical upward subcooled boiling flows in an internally heated annulus. The annulus channel consisted of an inner heater rod with a diameter of 19.1 mm and an outer round pipe with an inner diameter of 38.1 mm, and the hydraulic equivalent diameter was 19.1 mm. The double-sensor conductivity probe method was used for measuring local void fraction, interfacial area concentration, and interfacial velocity. A total of 11 data were acquired consisting of four inlet liquid velocities, 0.500, 0.664, 0.987 and 1.22 m/s and two inlet liquid temperatures, 95.0 and 98.0 $^{\circ}$ C. The constitutive equations for distribution parameter and drift velocity in the drift-flux model, and the semi-theoretical correlation for Sauter mean diameter, namely, interfacial area concentration, which were proposed previously, were validated by local flow parameters obtained in the experiment. $© 2004 Elsevier Ltd. All rights reserved.$

Keywords: Void fraction; Interfacial area concentration; Drift-flux model; Subcooled boiling flow; Multiphase flow; Internally heated annulus

1. Introduction

The capability to predict the void fraction and the interfacial area concentration in subcooled boiling region is of considerable interest to boiling water reactor (BWR) safety. This is because the void fraction significantly affects the reactor power and the interfacial area concentration is one of the important parameters that

determine the heat transfer capability and the possible occurrence of critical heat flux. The existence of the thermodynamic non-equilibrium between the phases complicates the analysis of the subcooled boiling flow. The extensive literature reviews on subcooled boiling flow researches were performed by Rogers and Li [1], Lee and Bankoff [2], and the present authors [3]. The literature reviews covered both correlations and phenomenological models and attempted to point out the major assumptions and methods applied to developing these models. From the literature reviews, it has turned out that most existing models or correlations are applicable only to limited experimental conditions. It can also be seen that there is limited local data and no local data concerning interfacial area concentration distribution

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Nomenclature

for subcooled boiling flow. Consequently, it is desirable to establish a database of local interfacial parameters. It is also required to develop reliable constitutive models for broad subcooled boiling conditions.

The purpose of this study is the continued enhancement of the safety of the current generation of BWRs. In this study, local measurements of two-phase flow parameters such as void fraction, interfacial area concentration and interfacial velocity are conducted in subcooled boiling flows in an experimental loop. The extensive discussions are performed to examine the dependence of inlet liquid temperature, heat flux and inlet liquid velocity on local flow parameters. The obtained data are also used for evaluating the applicability of existing drift-flux model and interfacial area correlation to subcooled boiling flow.

2. Experimental

An experimental facility was designed to measure the relevant two-phase parameters necessary for developing constitutive models for the two-fluid model in subcooled boiling. It was scaled to a prototypic BWR based on scaling criteria for geometric, hydrodynamic, and thermal similarities [3]. The scaling criteria used to design the test loop are detailed in Appendix A. The experimental facility, instrumentation, and data acquisition system are briefly described in this section.

[Fig. 1](#page-2-0) shows the experimental facility layout. The water supply is held in the holding tank. The tank is open to the atmosphere through a heat exchanger mounted to the top to prevent explosion or collapse and to degas from the water. There is a cartridge heater inside the tank to heat the water and maintain the inlet water temperature. A cooling line runs inside the tank to provide control of the inlet subcooling and post-experimental cooling of the tank. Water is pumped with a positive displacement, eccentric screw pump, capable of providing a constant head with minimum pressure oscillation. The water, which flows through a magnetic flow meter, is divided into four separate flows and can then be injected into the test section. The test section is an annular geometry that is formed by a clear polycarbo-

Fig. 1. Schematic diagram of experimental loop.

nate pipe on the outside and a cartridge heater on the inside. The test section is 38.1 mm inner diameter and has a 3.18 mm wall thickness. The overall length of the heater is 2670 mm and has a 19.1 mm outer diameter. The heated section of the heater rod is 1730 mm long. The heater rod has one thermocouple that is connected to the process controller to provide feedback control. A pressure tap and thermocouple are placed at the inlet and exit of the test section. A differential pressure cell is connected between the inlet and outlet pressure taps. The two-phase mixture flows out of the test section to a separator tank and the vapor phase is drained away. The water is returned to the holding tank. There are several operation limits about the experimental loop that should be noted. The limits are the flow rate of the liquid $(143-2010 \text{ kg/(m}^2 \text{ s})$ at 100 °C), the maximum heat flux (0.193 MW/m^2) , the maximum cooling capacity (29 kW), and the inlet subcooling $(2.2-26 \degree C)$.

There are several K-type thermocouples used in the experimental loop. The uncorrected error of these thermocouples is ± 2.2 °C. A thermocouple measures the temperature in the main tank. There are two thermocouples inserted into the inlet and outlet flanges of the test section. Finally, there is a thermocouple inside the heater rod to provide a feedback to the heater controller. The test section inlet temperature is measured by a thermistor probe with interchangeable sensor accuracy of ± 0.1 °C. A magnetic flow meter is used to measure the average fluid flow rate entering the test section. The magnetic flow meter has an accuracy of $\pm 1\%$. The

differential pressure between the inlet and outlet of the test section is measured with a Honeywell ST 3000 Smart Transmitter. The combined zero and span inaccuracy for this differential pressure cell is 0.4% of span. Silicon-controlled rectifier (SCR) is used to control the heat flux. The SCR uses zero-voltage-switching that controls the load by controlling the number of completed sine waves. Because only whole sine waves are used and the power is switched when the sine wave crosses zero, there exists minimal radio frequency interference.

The double point electrical conductivity probe is used to make the two-phase parameter measurements including void fraction, interfacial area concentration, and interfacial velocity. The diameter of the probe tip is less than 0.002 mm. The double sensor probe methodology was detailed in our previous paper [4], and the measurement accuracies for void fraction, interfacial area concentration and interfacial velocity were estimated to be $\pm 12.8\%$, $\pm 6.95\%$ and $\pm 12.9\%$, respectively [4]. There is an electrical double-sensor conductivity probe at the axial location of $z_h/D_H = 52.6$. The radial distributions of the flow parameters were obtained by traversing the double sensor probe along the radial direction. The radial locations measured by the probe are from r/ $(R - R_0) = 0.05{\text{-}}0.95$, where $r/(R - R_0) = 0$ and 1 correspond to the surface of the inner rod and outer pipe, respectively. The flow conditions in this experiment are tabulated in [Table 1](#page-3-0).

3. Results and discussion

3.1. Measured flow parameters

[Figs. 2–5](#page-4-0) show the radial distributions of local void fraction, interfacial area concentration, interfacial velocity, and bubble Sauter mean diameter, respectively. In each figure, upper (a), middle (b), and lower (c) figures show the radial distributions of flow parameters displayed as a fixed parameter of heat flux, inlet liquid temperature, and inlet liquid velocity, respectively.

As expected in subcooled boiling flow, a sharp peaking close to the heater surface is observed in the void fraction distributions, see [Fig. 2.](#page-4-0) The void fraction reaches maximum around $r/(R - R_0) = 0.1$, i.e., 0.95 mm from the heater surface. [Fig. 5](#page-7-0) shows that maximum local bubble diameters are around 2 mm. Thus, the peak position of the void fraction roughly corresponds to the maximum bubble radius. Since the bulk subcooling increases along the radial direction, the bubbles collapse and the void fraction drops along the radial direction sharply. [Fig. 2](#page-4-0) shows the dependence of void fraction profile on thermal and flow parameters. As the heat flux increases, the void fraction not only increases in value, but also propagates along the radial direction, see [Fig.](#page-4-0) [2](#page-4-0)(a). The effect of increasing inlet temperature or

decreasing inlet liquid velocity has the similar consequence, see [Fig. 2](#page-4-0)(b) and (c), respectively. [Fig. 2](#page-4-0) also indicates the existence of a bubble layer in subcooled boiling, that is, the flow can be characterized as two distinctive flow regions, boiling two-phase (bubble layer) region and liquid single-phase region [5]. As heat flux increases, inlet temperature increases, or inlet liquid velocity decreases, the bubble layer thickness increases.

As shown in [Fig. 3](#page-5-0), the radial distribution of interfacial area concentration exhibits the similar behavior to that of void fraction. The local interfacial area concentration reaches the peak around $r/(R - R_0) = 0.1$, and then drops significantly along the radial direction. The effects of thermal and flow parameters on the interfacial area concentration are also similar to those on the void fraction, that is, the interfacial area concentration increases as heat flux increases, or inlet temperature increases, or inlet liquid velocity decreases.

As shown in [Fig. 4,](#page-6-0) for most of the experimental conditions, the local interfacial velocity profiles are found to be almost flat in the region where the radial location is roughly smaller than the local bubble Sauter mean diameter, namely, $r \leq D_{\text{Sm,max}}$. Since the bubbles in the region are expected to slide on the heater surface, the flat interfacial velocity profile in the bubble-layer region may mainly be due to the sliding bubbles on the heater surface. For $r > D_{\text{Sm,max}}$, the interfacial velocity gradually increase along the radial direction, and may reach its maximum value around the channel center. The inlet liquid Reynolds numbers varies in the experiments from 28,870 to 70,260, which means that the flows are essentially turbulent flow. Thus, the liquid velocity profile is expected to be quite flat around the channel center. Therefore, the increase in the interfacial velocity along the radial direction around the channel center may not be so significant.

The flow and thermal parameters affect the distribution of interfacial velocity profile. [Fig. 4](#page-6-0)(a) and (b) indicates that the increase of the heat flux increases the interfacial velocity and the increase of the inlet liquid temperature increases the interfacial velocity, respectively. The increase of the heat flux or the inlet liquid temperature increases the void fraction, resulting in the liquid velocity. Thus, the increase of the interfacial velocity may mainly be attributed to the increased void fraction. [Fig. 4](#page-6-0)(c) shows the dependence of the inlet liquid flow rate on the interfacial velocity. Unlike the dependence of the heat flux or the inlet liquid temperature on the interfacial velocity, the effect of the inlet liquid velocity on the interfacial velocity may not be clear in the vicinity of the heater surface in some experimental conditions. The increase in the liquid velocity certainly tends to increase the interfacial velocity, since the interfacial velocity is basically the sum of the liquid velocity and the relative velocity between phases. On the other hands, the increase in the liquid velocity keeping the heat flux and the inlet liquid velocity constant decreases the void fraction, see [Fig. 2](#page-4-0)(c). Thus, the systematic effect of the liquid velocity on the interfacial velocity is not obtained particularly in the vicinity of the heater surface.

As expected in subcooled boiling flow, a sharp increase close to the heater surface is observed in the bubble Sauter mean diameter distributions, see [Fig. 5.](#page-7-0) At low void fraction conditions, the distribution profile of the bubble diameter along the radial direction is similar to that of the void fraction. This indicates that bubbles collapse in the subcooled bulk region due to high liquid subcooling. On the other hand, at higher void fraction condition, such as the condition with $T_{\text{in}} = 98.0 \text{ °C}$, $q = 100$ kW/m², and $v_{\text{f,in}} = 0.499$ m/s, the void fraction keeps dropping along the radial direction even at the outer half of the channel. However, the bubble diameter is still about 2 mm even in the vicinity of the outer channel wall. This suggests that the bulk temperature is around saturate temperature and thus bubbles would not collapse. The effects of flow and thermal parameters on the radial profile of Sauter mean diameter is similar to those on the void fraction profile, that is, as heat flux increases, or inlet temperature increases, or inlet liquid

Fig. 2. Local void fraction profiles as a parameter of: (a) heat flux; (b) inlet liquid temperature; (c) inlet liquid velocity.

velocity decreases, the Sauter mean diameter will increase.

[Figs. 6 and 7](#page-8-0) show the dependence of the area-averaged void fraction on the thermal equilibrium quality and the dependence of the area-averaged Sauter mean diameter on the thermal equilibrium quality, respectively. These figures imply that the area-averaged void fraction and bubble Sauter mean diameter can closely be related to the thermal equilibrium quality. When the

thermal equilibrium quality is less than -0.013 , the void fraction is negligibly small, see [Fig. 6](#page-8-0). As the thermal equilibrium quality increases, the void fraction increases significantly, and it reaches 0.17 when quality is -0.0012 . When the thermal equilibrium quality is less than -0.017, the bubble Sauter mean diameter is almost zero, see [Fig. 7](#page-8-0). As the thermal equilibrium quality increases, the bubble diameter increases gradually, and it reaches about 3 mm when the thermal equilibrium quality is 0.

Fig. 3. Local interfacial area concentration profiles as a parameter of: (a) heat flux; (b) inlet liquid temperature; (c) inlet liquid velocity.

3.2. Constitutive equations of void fraction and interfacial area concentration

The void fraction and interfacial area concentration are two fundamental geometrical parameters in a bubbly two-phase flow. The void fraction expresses the phase distribution and is a required parameter for hydrodynamic and thermal design in various industrial processes. On the other hand, the interfacial area concentration describes available area for the interfacial transfer of mass, momentum and energy, and is a required parameter for a two-fluid model formulation. Various transfer mechanisms between phases depend on the two-phase interfacial structures. Therefore, an

Fig. 4. Local interfacial velocity profiles as a parameter of: (a) heat flux; (b) inlet liquid temperature; (c) inlet liquid velocity.

accurate knowledge of these parameters is necessary for any two-phase flow analyses. This fact can further be substantiated with respect to two-phase flow formulation. In what follows, the constitutive equations for distribution parameter and drift velocity in the drift-flux

model, and the semi-theoretical correlation for Sauter mean diameter namely interfacial area concentration, which were proposed previously, were validated by area-averaged flow parameters obtained by integrating local flow parameters over the flow channel.

Fig. 5. Local Sauter mean diameter profiles as a parameter of: (a) heat flux; (b) inlet liquid temperature; (c) inlet liquid velocity.

3.2.1. Constitutive equation of void fraction—Drift-flux model

The drift-flux model is one of the most practical and accurate models for two-phase flow. The applicability of the existing constitutive equations for the distribution parameter and drift velocity in the drift-flux model to subcooled boiling flow will be examined by the data obtained in this study. The one-dimensional drift-flux model is given by [6]

$$
\langle \langle v_{g} \rangle \rangle = \frac{\langle \alpha v_{g} \rangle}{\langle \alpha \rangle} = \frac{\langle j_{g} \rangle}{\langle \alpha \rangle} = \frac{\langle \alpha j \rangle}{\langle \alpha \rangle \langle j \rangle} \langle j \rangle + \frac{\langle \alpha v_{gj} \rangle}{\langle \alpha \rangle}
$$

= $C_{0} \langle j \rangle + V_{gj},$ (1)

Fig. 6. Dependence of area-averaged void fraction on thermal equilibrium quality.

where v_{gi} is the drift velocity of a gas phase defined as the velocity of the gas phase with respect to the volume center to the mixture. The distribution parameter, C_0 , and the void-fraction-weighted mean drift velocity, V_{gi} , are defined as

$$
C_0 \equiv \frac{\langle \alpha j \rangle}{\langle \alpha \rangle \langle j \rangle} \quad \text{and} \quad V_{\text{gj}} = \frac{\langle \alpha v_{\text{gj}} \rangle}{\langle \alpha \rangle}.
$$
 (2)

Ishii [7] developed the constitutive equation of the distribution parameter in developing flow due to boiling in a round pipe as

$$
C_0 = \left(1.2 - 0.2\sqrt{\rho_g/\rho_f}\right) \left(1 - e^{-18\langle\alpha\rangle}\right). \tag{3}
$$

Recently, Hibiki et al. [5] successfully derived the constitutive equation of the distribution parameter in developing flow due to boiling in an internally-heated annuls from Eq. (3) by considering the difference in the channel geometry as

$$
C_0 = \left(1.2 - 0.2\sqrt{\rho_g/\rho_f}\right) \left[1 - \exp(-3.12 \langle \alpha \rangle^{0.212})\right].
$$
 (4)

On the other hand, Ishii [7] developed the constitutive equation of the void-fraction-weighted mean drift velocity in bubbly flow regime as

$$
V_{\rm gi} = \sqrt{2} \left(\frac{g \sigma \Delta \rho}{\rho_{\rm f}^2} \right)^{1/4} (1 - \langle \alpha \rangle)^{1.75}.
$$
 (5)

From Eqs. [\(1\), \(4\) and \(5\)](#page-7-0), the one-dimensional drift flux model can be recast in the following form

Fig. 7. Dependence of area-averaged bubble Sauter mean diameter on thermal equilibrium quality.

The above equation indicates that the superficial gas velocity is a function of the void fraction at a fixed superficial liquid velocity in a certain fluid system.

The distribution parameter and the drift velocity can be determined from Eq. (2) experimentally, provided that local void fraction and gas and liquid velocities are available. In this study, since no local liquid velocity data are available, the profile of the mixture volumetric flux in the estimation of the distribution parameter using measured local void fraction is approximated by

$$
j = \frac{n+1}{n} \langle j \rangle \left\{ 1 - \left| 1 - \frac{2r}{R - R_0} \right|^n \right\}.
$$
 (7)

Since the profile of mixture volumetric flux is expected to be more or less a power-law profile in a turbulent flow, the approximated profile of the mixture volumetric flux may not affect the estimation of the distribution parameter significantly [4,5]. This means that the void fraction profile is a dominant parameter to determine the distribution parameter in a turbulent flow. Thus, *n* is assumed to be 7 in this study [5].

The distribution parameters estimated by measured local void fraction and assumed mixture volumetric flux are compared with the existing constitutive equation, Eq. (4), in [Fig. 8.](#page-9-0) In the figure, open circles, and solid, broken, and dotted lines indicate the experimentally determined distribution parameters, the asymptotic value of the distribution parameter at $\langle \alpha \rangle = 1$ calculated by Eq. (3), the distribution parameter calculated by Eq.

$$
\langle j_{g} \rangle = \frac{\left(1.2 - 0.2\sqrt{\rho_{g}/\rho_{f}}\right) \left\{1 - \exp(-3.12 \langle \alpha \rangle^{0.212})\right\} \langle j_{f} \rangle + \sqrt{2} \left(\frac{\Delta \rho g \sigma}{\rho_{f}^{2}}\right)^{1/4} (1 - \langle \alpha \rangle)^{1.75}}{1/\langle \alpha \rangle - \left(1.2 - 0.2\sqrt{\rho_{g}/\rho_{f}}\right) \left\{1 - \exp(-3.12 \langle \alpha \rangle^{0.212})\right\}}.
$$
\n(6)

Fig. 8. Dependence of distribution parameter on void fraction in subcooled boiling flow.

[\(4\),](#page-8-0) and the distribution parameter calculated by Eq. [\(3\)](#page-8-0), respectively. As can be seen from Fig. 8, Eq. [\(4\)](#page-8-0) can reproduce the dependence of the distribution parameter on the void fraction properly. This may be attributed to the proper modeling of the distribution parameter, Eq. [\(4\),](#page-8-0) by considering the flow developing process in subcooled boiling flow [5]. The average relative deviation between Eq. [\(4\)](#page-8-0) and the distribution parameters estimated experimentally is estimated to be $\pm 4.83\%$.

In Fig. 9, the superficial gas velocities are plotted against the void fractions as a parameter of the superficial liquid velocity. The superficial liquid velocity is calculated by

$$
\langle j_{\rm f} \rangle = (G - \rho_{\rm g} \langle j_{\rm g} \rangle) / \rho_{\rm f}.
$$
 (8)

Fig. 9. Dependence of superficial gas velocity on void fraction in subcooled boiling flow.

In the figure, open symbols, solid, broken, dotted and chain lines indicate the measured superficial gas velocities, and the superficial gas velocities calculated by Eq. (6) for $v_{\text{fin}} = 0.500, 0.664, 0.985$ and 1.22 m/s, respectively. As can be seen from Fig. 9, the drift-flux model with Eqs. [\(4\) and \(5\)](#page-8-0) can reproduce the dependence of the superficial gas velocity on the void fraction properly. This may be mainly attributed to the proper modeling of the distribution parameter, since the contribution of the drift velocity to the gas velocity may not be significant in the present flow conditions. The average relative deviation between Eq. (6) and the measured superficial gas velocity is estimated to be ± 6.92 %. The comparisons shown in Figs. 8 and 9 suggest that the drift-flux model with Eqs. [\(4\) and \(5\)](#page-8-0) can be applicable to subcooled boiling flow in an internally heated annulus. However, the validity of the constitutive equation for the drift velocity should be examined separately by local flow data of gas and liquid phases to be measured in a future study.

The constitutive equation of the distribution parameter, Eq. [\(4\),](#page-8-0) and the drift-flux model, Eq. (6) are also evaluated by existing data. Lee et al. [8] conducted local flow measurements of subcooled water boiling flow in an internally heated annulus. The outer diameter of a heated inner pipe and the inner diameter of an outer pipe were 19.0 and 37.5 mm, respectively. In their experiment, a total of 18 data sets were acquired consisting of the mass flux, $476-1061 \text{ kg/m}^2$ s, the heat flux, $114.8-$ 320.4 kW/m², and the inlet subcooling, 11.5–21.3 °C. Eqs. [\(4\) and \(6\)](#page-8-0) can predict the distribution parameters and the superficial gas velocities within an average relative derivation of ±9.73% and ±4.20%, respectively. Roy et al. [9] also performed local flow measurements of subcooled R-113 boiling flow in an internally heated annulus. The outer diameter of a heated inner pipe and the inner diameter of an outer pipe were 15.9 and 38.1 mm, respectively. The experiments were carried out at the mass flux, 579 and 801 kg/m² s, the heat flux, 79.4– 126.0 kW/m², and the wall temperature 95-102 °C. A total of 7 complete data sets to calculate the distribution parameter and the other flow parameters are available in the paper. Eqs. [\(4\) and \(6\)](#page-8-0) can predict the distribution parameters and the superficial gas velocities within an average relative derivation of $\pm 27.5\%$ and $\pm 10.7\%$, respectively. Although the available data supports the validity of Eqs. [\(4\) and \(6\),](#page-8-0) extensive efforts to take local flow data should be encouraged to evaluate the constitutive equations in a future study.

3.2.2. Constitutive equation of interfacial area concentration and bubble diameter

Recently, Hibiki and Ishii [10] developed the constitutive equation of the interfacial area concentration under steady fully-developed adiabatic bubbly flow conditions based on the interfacial area transport equation as follows:

$$
\langle \tilde{a}_{i} \rangle = 3.02 \tilde{L} \sigma^{0.335} \langle \alpha \rangle \tilde{R} e^{0.239} \quad \text{or}
$$

$$
\langle \tilde{D}_{Sm} \rangle = 1.99 \tilde{L} \sigma^{-0.335} \tilde{R} e^{-0.239},
$$
 (9)

where

$$
\langle \tilde{a}_{i} \rangle \equiv \langle a_{i} \rangle Lo, \quad Lo \equiv \sqrt{\frac{\sigma}{g\Delta\rho}}, \quad \tilde{L}o \equiv \frac{Lo}{D_{\rm H}},
$$

$$
\tilde{R}e \equiv \frac{(\langle \varepsilon \rangle^{1/3}Lo^{1/3})Lo}{v_{\rm f}}, \quad \text{and} \quad \langle \tilde{D}_{\rm Sm} \rangle \equiv \frac{(6\alpha/a_{i})}{Lo} = \frac{\langle D_{\rm Sm} \rangle}{Lo}.
$$

The energy dissipation rate per unit mass in Eq. (9) is approximated by [8]

$$
\langle \varepsilon \rangle = g \langle j_{g} \rangle \exp(-AR_{\text{er}}) + \frac{\langle j \rangle}{\rho_{\text{m}}} \left(-\frac{\text{d}P}{\text{d}z} \right)_{\text{f}} \{1 - \exp(-AR_{\text{er}}) \},\tag{10}
$$

where g, A, Re_f , ρ_m , and $(-dP/dz)$ _F refer to the gravitational acceleration, a coefficient (=0.0005839), Reynolds number of the liquid phase defined by $\langle j_f \rangle D_H/v_f$, the mixture density, and the pressure loss per unit length due to friction, respectively. Although the applicability of Eq. (9) to developing flows was also confirmed experimentally [10], the applicability of Eq. (9) to subcooled boiling flow has not been examined because of very limited available data. It should be noted here that the heat flux does not appear in Eq. (9) explicitly. However, since the superficial gas and liquid velocities depend on the heat flux, the bubble diameter is certainly dependent on the heat flux.

In Fig. 10, Sauter mean diameters obtained by measured void fractions and interfacial area concentrations are compared with Eq. (9). In the figure, open circles and solid line indicate the measured bubble Sauter mean diameter non-dimensionalized by Laplace length and non-dimensional Sauter mean diameter calculated by Eq. (9), respectively. An excellent agreement is obtained

Fig. 10. Comparison of semi-theoretical correlation for Sauter mean diameter with experimental data.

between Eq. (9) and the data within an average relative deviation of $\pm 28.3\%$. This suggests that the constitutive equations given by Eq. (9) can be applicable to subcooled boiling flow in an internally heated annulus.

The constitutive equation of the bubble Sauter mean diameter, Eq. (9) is also evaluated by the R-113 data taken by Roy et al. [9] existing data. Only one complete data to calculate the bubble Sauter mean diameter and the other flow parameters is available at the mass velocity of 801 kg/m² s, the heat flux of 115.8 kW/m², and the inlet R-113 temperature of 43.0 °C. Eq. (9) can predict the bubble Sauter mean diameter with a relative derivation of ±25.0%. Although the available data supports the validity of Eq. (9), extensive efforts to take local flow data should be encouraged to evaluate the constitutive equation in a future study.

4. Conclusions

Local measurements of flow parameters were performed for vertical upward subcooled boiling flows in an internally heated annulus. The annulus channel consisted of an inner heater rod with a diameter of 19.1 mm and an outer round pipe with an inner diameter of 38.1 mm, and the hydraulic equivalent diameter was 19.1 mm. The double-sensor conductivity probe method was used for measuring local void fraction, interfacial area concentration, and interfacial velocity. The obtained results are summarized below:

- (1) A total of 11 data were acquired consisting of four inlet liquid velocities, 0.500, 0.664, 0.987 and 1.22 m/s and two inlet liquid temperatures, 95.0 and 98.0 $^{\circ}$ C.
- (2) The dependence of the local flow parameters on the heat flux, the inlet liquid temperature, and the inlet liquid velocity were discussed in detail.
- (3) The constitutive equation for the distribution parameter in the drift-flux model proposed previously was evaluated by local flow parameters obtained in the experiment. The constitutive equation for the distribution parameter could predict the experimentally determined distribution parameter within an average relative deviation of $\pm 4.83\%$. The drift flux model with the validated constitutive equations for the distribution parameter could also predict the experimental data within an average relative deviation of ±6.92%.
- (4) The semi-theoretical correlation for Sauter mean diameter, namely, interfacial area concentration proposed previously was validated by local flow parameters obtained in the experiment. The correlation for Sauter mean diameter could predict the measured Sauter mean diameter within an average relative deviation of ±23.9%.

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Appendix A

The scaling criteria for two-phase flow loops have been developed by Ishii and his colleagues [11–14]. In what follows, the important scaling criteria for twophase flow will be explained briefly by taking the convective boiling flow under the subcooled condition in the BWR core as an example. The prototypic conditions in the BWR core are a system pressure of 7.17 MPa and a water temperature that changes from 278 °C at the inlet to the saturation temperature 287 °C . The prototypic conditions in the BWR core is simulated by an atmospheric pressure loop using water as the coolant based on the scaling method, which provides similar geometric, hydrodynamic, and thermal characteristics as those found in the prototype.

The non-dimensional parameters specifying similar hydraulic and thermal characteristics of the flow are obtained from the scaling method. These non-dimensional parameters include the Reynolds number and the Weber number. However, it is almost impossible to satisfy all the flow characteristics because each flow property depends on the fluid properties and the fluid properties are different. This is particularly true when the flow has more than one phase such as a vapor/liquid flow. For the vapor/liquid flow the geometrical similarity is important, i.e., the relative size of the bubble to the channel structure. A large deviation of the geometrical conditions from the flow in the prototype induces a significant change in the vapor phase distribution and could even results in a different flow regime. Therefore, the geometrical similarity is used as the first scaling criteria.

There are some parameters that are determined only by the fluid properties and not by the hydrodynamic conditions. For example, the constitutive equations for the bubble diameter imply that the bubble size can be estimated by the fluid properties. Also the relative velocity between the bubble and the continuous phase can be expressed as a function of the flow properties. Although the relative velocity does not affect directly the geometrical parameters, it has a significant role in the calculation of the void fraction distribution. Therefore the parameters that can not be controlled by the design parameters should be evaluated.

A.1. Geometrical similarity

The ratio of the bubble diameter to the heating rod diameter should be scaled as

$$
\left[\frac{D_{\rm b}}{D_{\rm rod}}\right]_{\rm R} = 1.\tag{A.1}
$$

Similarly the ratio of the bubble diameter to the hydraulic diameter should be scaled as

$$
\left[\frac{D_{\rm b}}{D_{\rm H}}\right]_{\rm R} = 1,\tag{A.2}
$$

where the subscript R denotes the ratio of the value for a model to that of the prototype

$$
\psi_{\rm R} \equiv \frac{\psi_{\rm m}}{\psi_{\rm p}} = \frac{\psi \text{ for model}}{\psi \text{ for prototype}}.
$$
\n(A.3)

Both criteria, Eqs. (A.1) and (A.2) are effective in the bubble layer development for subcooled convection boiling flow. To estimate the heating rod diameter and the hydraulic diameter in the model, we may approximate the bubble diameter as

$$
D_{\rm b} \approx \frac{D_{\rm b,max}}{2},\tag{A.4}
$$

where $D_{\text{b,max}}$ is the maximum distorted bubble limit given by [15]

$$
D_{\text{b,max}} = 4\sqrt{\frac{\sigma}{g\Delta\rho}}.\tag{A.5}
$$

A.2. Hydrodynamic similarity

The ratio of the relative velocity to the liquid velocity should be scaled as

$$
\left[\frac{v_r}{v_f}\right]_{\mathbf{R}} = 1.\tag{A.6}
$$

To estimate the liquid velocity in the model, we may approximate the bubble rise velocity, v_r , as [15]

$$
v_{\rm r} \approx \sqrt{2} \left(\frac{\sigma g \Delta \rho}{\rho_{\rm r}^2} \right)^{1/4}.
$$
 (A.7)

A.3. Thermal similarity

Subcooled number, N_{sub} , and Zuber number (phase change number), N_{Zu} , play an important role in the thermal similarity criteria. The subcooled number is the ratio of the subcooling to the latent heat as

$$
N_{\rm sub} = \frac{\Delta h_{\rm sub}}{h_{\rm fg}} \left(\frac{\Delta \rho}{\rho_{\rm g}}\right),\tag{A.8}
$$

where $\Delta h_{\rm sub}$ and $h_{\rm fg}$ are the subcooling enthalpy and the latent heat, respectively. The Zuber number is the ratio of the heat flux used for phase change over the inlet subcooling as

$$
N_{\text{Zu}} = \frac{4qL_{\text{h}}}{D_{\text{H}}v_{\text{f,in}}h_{\text{fg}}\rho_{\text{f}}} \left(\frac{\Delta\rho}{\rho_{\text{g}}}\right),\tag{A.9}
$$

where L_h is the heated length.

Table 2

Prototypic BWR conditions and experimental conditions in the present experiment

Quantity	Prototype	Model
Pressure (MPa)	7.17	0.101
Saturation temperature $(^{\circ}C)$	287	100
Heater diameter (m)	0.0123	0.0191
Hydraulic diameter (m)	0.0150	0.0191
Heated length (m)	3.81	1.73
Heater power (kW)	77.2	20.0
Heat flux $(kW/m2)$	526	193
Bubble size (mm)	3.18	5.01
$D_{\rm b}/D_{\rm H}$ (-)	0.212	0.263
Bubble rise velocity (m/s)	0.172	0.222
Liquid inlet velocity (m/s)	1.93	$0.498 - 1.24$
Reynolds number $(-)$	2.24×10^{5}	$3.22 \times 10^4 - 8.05 \times 10^4$
Weber number $(-)$	4.00	4.00
Subcooling number $(-)$	0.650	$5.99 - 15.0$
Zuber (phase change) number $(-)$	4.72	$7.61 - 20.5$
Inlet subcooling $(^{\circ}C)$	9.49	$2.00 - 5.00$
$[D_{\rm b}/D_{\rm rod}]_{\rm R}$		1.01
$[D_{\rm b}/D_{\rm H}]_{\rm R}$		1.24
$[We]_R$		1.00
$[v_r/v_f]_R$		$0.200 - 0.498$
$[N_{sub}]_R$		$9.21 - 23.0$
$[N_{\rm Zu}]_{\rm R}$		$1.61 - 4.34$
$[x_{\text{eq}}]_{\text{R}}[\Delta\rho/\rho_{g}]_{\text{R}}$		$-1.88 - 2.88$

From the steady state energy equation balanced over the heated section using a control volume analysis, N_{sub} and N_{Zu} are related by

$$
\left(\frac{\Delta \rho}{\rho_{\rm g}}\right) x_{\rm eq.} = N_{\rm Zu} - N_{\rm sub}.\tag{A.10}
$$

Therefore, the similarity of the subcooling and Zuber numbers yields

$$
[x_{\text{eq.}}]_{\text{R}} \left[\frac{\Delta \rho}{\rho_{\text{g}}} \right]_{\text{R}} = 1. \tag{A.11}
$$

This indicates that the vapor quality should be scaled by the density ratio.

Some of the important scaling criteria are highlighted as described above, and the detailed discussions on the scaling criteria are found in the previous papers [11– 15]. The loop geometry and the thermal-hydraulic conditions in the prototypic BWR and the scaled model are tabulated in Table 2. In the test loop used in the present experiment, the geometrical similarity is almost preserved, but hydrodynamic and thermal similarities are not completely preserved due to the limited capability of the test equipment. The typical ranges of the similarity parameters covered in the present experiment are also tabulated in Table 2. Thus, since the geometrical similarity, namely the bubble migration characteristics is preserved in the present experiment, the obtained data would provide the information on more general

basic flow characteristics in the channel of the BWR core rather than that at the operating condition of the BWR.

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